

Optimal Income Redistribution

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Motivation

- Two major elements of the modern welfare state:
 - Income tax-and-transfer system
 - Pay-as-you-go pension system
- Considerable heterogeneity across countries:
 - US: moderately progressive income tax system, not generous and strongly progressive pension system
 - Europe: progressive income tax system and generous, fairly linear pension system

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- Two major elements of the modern welfare state:
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- Considerable heterogeneity across countries:
 - US: moderately progressive income tax system, not generous and strongly progressive pension system
 - Europe: progressive income tax system and generous, fairly linear pension system
- Should both systems operate in tandem to achieve the desired levels of redistribution and insurance?
- Or would it be more efficient to streamline Social Security, as in many European countries?
- What can rationalize these differences? (future research)

What do we do?

- Set-up a state-of-the-art life-cycle model with realistic pension and tax-transfer systems.
- Compute the optimal combination of the pension system (in terms **generosity** and **progressivity**) and **income tax progressivity** under different welfare criteria.
- Key trade-offs:
 - Pension progressivity distorts labor supply (and hence human capital accumulation) of the high productivity agents more.
 - Pension generosity reduces labor supply distortions but financed by distortionary payroll taxes.
 - Both distort life-cycle savings and retirement decisions.
 - Redistribution within generations through progressivity (of pensions and taxes).
 - Redistribution across current and future generations comes through the time path of distortions.
 - Intergenerational links, welfare objectives, and transitions are key.

Literature

- ① **Optimal Pension Generosity and Progressivity** Nishiyama and Smetters (2007 JPE), Huggett and Parra (2010 JPE), Fehr, Kallweit & Kindermann (2013 JEEA), Brendler (2022 RED), Nam (2023)
 - ② **Optimal Income Tax Progressivity** Heathcote, Storesletten & Violante (2017 QJE), Conesa and Krueger (2007, JME), Conesa, Kitao, & Krueger (2009, AER), Guner, Kaygusuz & Ventura (2023 ECMA), Carroll, Luduvic & Young (2023), MacNamara & Rossi (2023)
- **We find significant welfare gains from joint reforms, however results and to the welfare objective.**
 - Some recent work on the joint income tax and pension systems:
 - Ludwig et al. (2023) → aging & solvency; Brendler (2023 JME) → inverse-optimum approach;
 - Makarski et al (2023) → complementing pension privatization with a tax reform;
 - Kindermann and Puschel (2023) → design pension progressivity like EITC
 - Tran and Zakariya (2023) → Pension progressivity through means testing

Findings

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- Pension generosity and progressivity are substitutes with income tax progressivity:
 - Providing less insurance through the pension system requires more insurance through the income tax system.
 - Intergenerational preferences determine the balance between overall insurance vs. distortions.

→ For any intergenerational preferences, we find joint reforms that make all current and future cohorts, on average, better off.

Model

Overview

- Overlapping generations with agents live up to max. age J but may die earlier ($\psi_j^{z,v}$ – education-, type- and age-specific survival rates).
- Agents enter at age $j = 1$ with permanent component of productivity v , no assets ($a_0=0$), and with an education level $z \in \{H, L\}$.
- Each education level comes with initial skill $h_{1,z}$ and (permanent) learning ability θ_z
- Agents accumulate skills through learning-by-doing (l – hours worked):

$$h_{j+1,z} = (1 - \delta^h) \cdot h_{j,z} + \theta_z \cdot (h_{j,z} \cdot l)^{\gamma^h}$$

- Retirement is endogenous with penalty for retiring early.
- Agents leave bequests due “joy of giving” preferences.

Worker's budget

- Pre-tax earnings ($w_{z,t}$ – skill price, v – fixed effect, y_j – idios. shock):

$$e = w_{z,t} \cdot h_{j,z} \cdot v \cdot y_j \cdot l$$

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- Budget constraint ($\lambda_{I,t}$ – income tax policy):

$$a' + (1 + \tau_c)c = (1 + r_t)a + e - \underbrace{\tau_{SS,t} \times \min(cap, e)}_{\text{Soc. Sec. taxes}} - \underbrace{\Psi_t(l; \lambda_{I,t})}_{\text{income taxes}}$$

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- Taxable income: $l = r_t a + e - \underbrace{0.5 \tau_{SS,t} \times \min(cap, e)}_{\text{Soc. Sec. deduction}}$

Retiree's budget

- Budget constraint ($\lambda_{SS,t}$ – Social Security policy):

$$a' + (1 + \tau_c)c = (1 + r_t)a + \underbrace{b(\bar{b}_t(\bar{e}; \lambda_{SS,t}), j^R)}_{\text{pension net of penalty}} - \underbrace{\max\{0, \Psi_t(\iota; \lambda_{I,t})\}}_{\text{income taxes}}$$

\bar{b}_t – normal pension benefit, j^R – retirement age, \bar{e} – average lifetime earnings

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\bar{b}_t – normal pension benefit, j^R – retirement age, \bar{e} – average lifetime earnings

- Taxable income:

$$\iota = \underbrace{r_t a}_{\text{asset income}} + \underbrace{b}_{\text{pension}}$$

Household's problem

- Individual state space: $\mathbf{x} = (j, v, z, y, h, \bar{e}, a, j^R)$

j – age, v – fixed effect, z – education, y – idios. shock,

h – human capital, a – assets, j^R – retirement age,

$\bar{e}_{j+1} = [(j - 1)\bar{e}_j + \min(e_j, cap)] / j$ – average lifetime earnings

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$\bar{e}_{j+1} = [(j - 1)\bar{e}_j + \min(e_j, cap)] / j$ – average lifetime earnings

- Worker's problem (no decision to retire):

$$V_t(\mathbf{x}) = \max_{\substack{c, a' \geq 0, \\ l \in [0, 1]}} \left\{ u(c, 1 - l) + \beta \psi_j^{z, v} \mathbb{E}_{y'|y} \left[\Gamma_{j+1, t+1}^{z, v} \int V_{t+1}(\mathbf{x}'_b) \Phi_{t+1}^{z, v}(b) db + \right. \right. \\ \left. \left. + (1 - \Gamma_{j+1, t+1}^{z, v}) V_{t+1}(\mathbf{x}') \right] + (1 - \psi_j^{z, v}) q(a') \right\}.$$

$\Gamma_{j+1, t+1}^{z, v}$: age and type dependent probability of receiving bequests; $\Phi_{t+1}^{z, v}(b)$: the distribution bequests left to type $(z, v) \Rightarrow$ **Intergenerational links of types.**

Government: Social Security

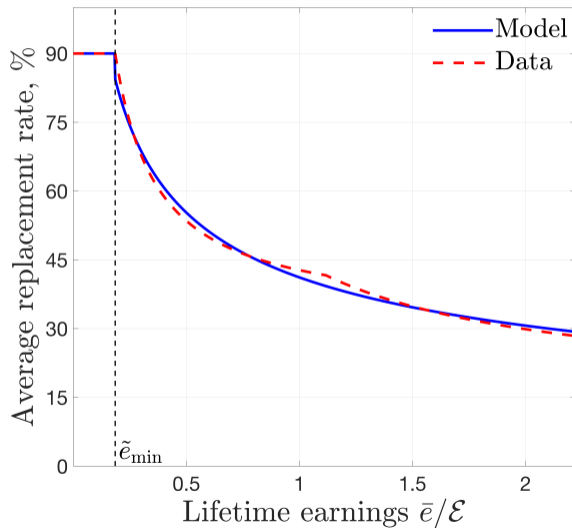
- Normal pension \bar{b}_t is determined by replacement rate schedule: $\bar{b}_t = R_t(\bar{e}; \lambda_{SS,t}) \cdot \bar{e}$
- Empirical schedule is approximated using:

$$R_t(\bar{e}; \lambda_{SS,t}) = \begin{cases} \bar{\lambda}_{SS,t} \times \bar{e}^{1-\lambda_{SS,t}} & \text{if } \bar{e} \geq \bar{e}_{\min} \\ \bar{\lambda}_{SS,t} \times \bar{e}_{\min}^{1-\lambda_{SS,t}} & \text{otherwise} \end{cases}$$

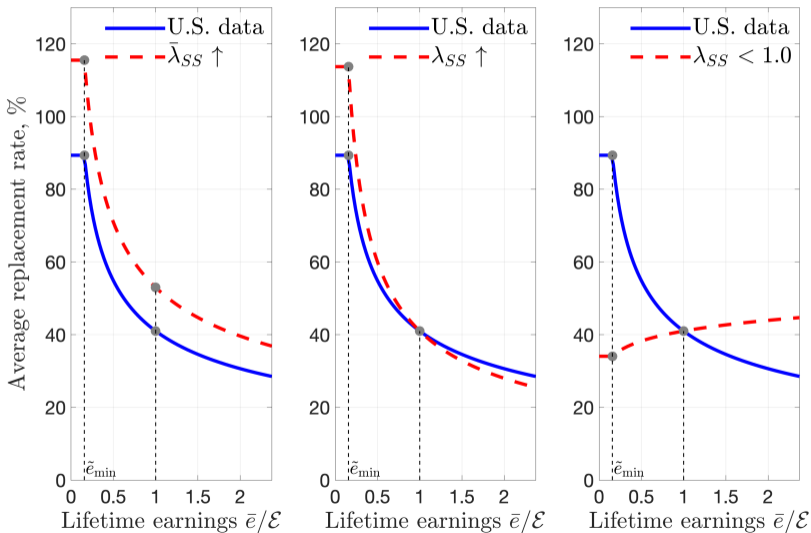
$\bar{\lambda}_{SS,t}$ – level (generosity), $\lambda_{SS,t}$ – curvature (progressivity), $\bar{e} = \bar{e} / \mathcal{E}_{t-j+j^R}$ with \mathcal{E}_{t-j+j^R} – economy-wide average lifetime earnings at retirement

- Penalty: $b(\bar{b}, j^R) = (1 - \delta^p) \cdot \bar{b} + \left(\frac{j^R - J^E}{J^R - J^E} \right) \cdot \delta^p \cdot \bar{b}$
- Given $(\bar{\lambda}_{SS,t}, \lambda_{SS,t})$, Social Security tax $\tau_{SS,t}$ adjusts each period to balance pay-as-you-go budget

Statutory replacement rate schedule



Government: Social Security



Government: Income taxation

- Net tax liability (HSV function):

$$\Psi_t(\iota; \bar{\lambda}_{I,t}, \lambda_{I,t}) = \iota - \mathcal{I}_t \cdot (1 - \bar{\lambda}_{I,t}) \cdot (\iota/\mathcal{I}_t)^{1-\lambda_{I,t}}$$

$\bar{\lambda}_{I,t}$ – income tax level, $\lambda_{I,t}$ – income tax progressivity, \mathcal{I}_t – aggregate taxable income

Government: Income taxation

- Net tax liability (HSV function):

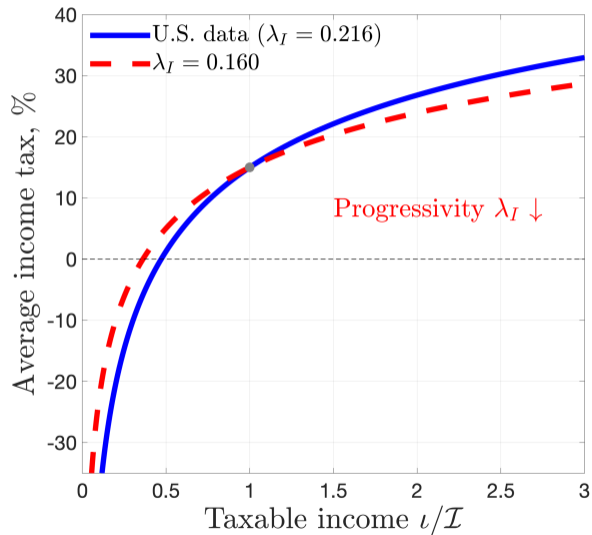
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$\bar{\lambda}_{I,t}$ – income tax level, $\lambda_{I,t}$ – income tax progressivity, \mathcal{I}_t – aggregate taxable income

- Income tax program runs a separate budget
- Given $\lambda_{I,t}$, income tax level $\bar{\lambda}_{I,t}$ balances the general government budget:

$$\begin{aligned} &\text{Income taxes} + \text{Consumption taxes} + \text{Debt issuance} \\ &= \text{Wasted spending} + \text{Debt service} \end{aligned}$$

Government: Income taxation



Firms and Equilibrium

- Standard production function allowing imperfect substitutability between skilled and unskilled workers

$$Y_t = ZK_t^{\varpi} \left[\left(N_{L,t}^{\rho} + N_{H,t}^{\rho} \right)^{\frac{1}{\rho}} \right]^{1-\varpi}$$

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$$Y_t = ZK_t^\varpi \left[\left(N_{L,t}^\rho + N_{H,t}^\rho \right)^{\frac{1}{\rho}} \right]^{1-\varpi}$$

- General Equilibrium
 - Labor markets and capital market clear.
 - Budget constraints for Social Security and general government clear.
 - Bequest distributions are internally consistent.
 - Any change in the tax system will trigger a transitional dynamics for the interest rate, wages, the average income tax rates and social security contribution rates.
 - They are key for welfare evaluations.

Calibration and Model Fit

Calibration

- We calibrate the model to the recent US data
- Agents enter the model at age 25
- Tax parameters are set to approximate current US income tax and social security system
- Earnings process is calibrated inside the model to match earnings and income distribution
- Learning by-doing technology is calibrated inside the model to match life-cycle profiles of hourly wages
- “Joy of giving” parameters are set to match the distribution of bequests.

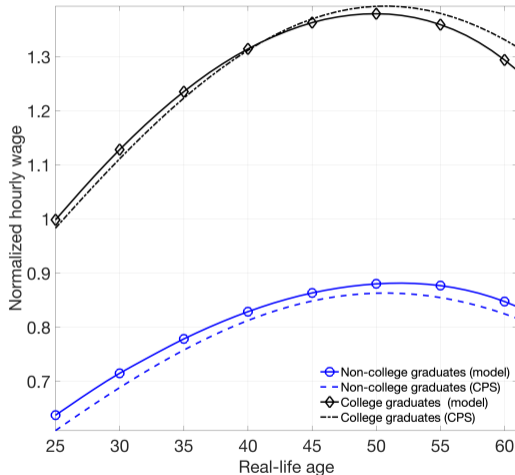
Externally calibrated parameters

Parameter	Description	Value
<u>Demographics and preferences</u>		
(J, J^E, J^R)	Maximum age, early and normal retirement age	(76, 38, 42)
$\{\psi_j^{z,v}\}$	Education and income specific age profile of survival probabilities	▶ Appendix
n	Population growth rate, %	1.3
σ	Coefficient of relative risk aversion	2.0
<u>Labor productivity</u>		
γ^h	Elasticity of human capital production	0.7
$(\rho_y, \sigma_\epsilon^2)$	Persistence and variance of AR(1) shock	(0.979, 0.015)
(π_z, π_v)	Inter-generational transmission of labor productivity	See text
<u>Production</u>		
(ϖ, δ)	Capital share and capital depreciation, %	(46.0, 6.0)
ρ	Elasticity of substitution is $1/(1 - \rho)$	0.285
<u>Government policies</u>		
λ_I	Income tax progressivity	0.216
λ_{SS}	Pension system progressivity	1.420
τ_c	Consumption tax, %	4.1
(dy, gy)	Debt-to-GDP and wasted spending-to-GDP ratio, %	(100.0, 7.8)

Internally calibrated parameters

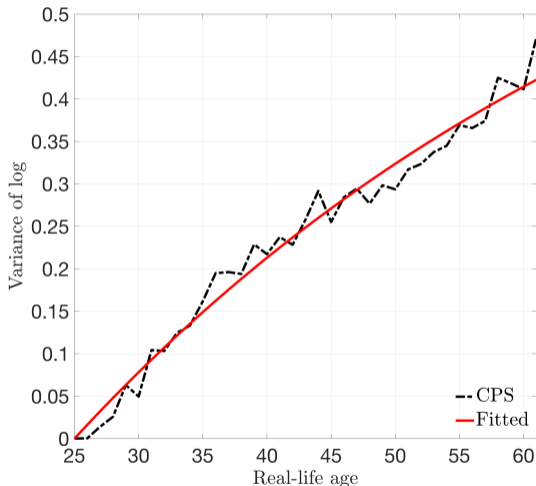
Parameter	Description and target	Value
<u>Preferences</u>		
β	Discount factor (Capital/GDP = 3.0)	0.99
γ	Weight on consumption (average hours = 0.40)	0.318
(ϕ_1, ϕ_2, η)	"Joy of giving" (Bequest distribution)	(8.0, 4.0, 2.3)
<u>Labor productivity</u>		
$(h_{1,H}, h_{1,L})$	Initial skill levels (hourly wage profiles)	(1.59, 0.45)
δ^h	Skill depreciation, % (hourly wage profiles)	5.9
σ_v^2	Var. of fixed effect (Gini for pre-gov. earnings = 0.40)	0.021
<u>Production</u>		
Z	TFP (average wage = 1.0)	0.263
<u>Government policies</u>		
$\bar{\lambda}_{SS}$	Replacement rate level ($\tau_{SS} = 10.6\%$)	0.413
\tilde{e}_{\min}	Lowest bend point	0.05
cap	Max. taxable earnings (taxable earnings > cap = 8%)	1.11
δ^p	Penalty for early retirement (retired at age 62 = 26%)	0.167 Details

Model fit: Life-cycle wage profiles



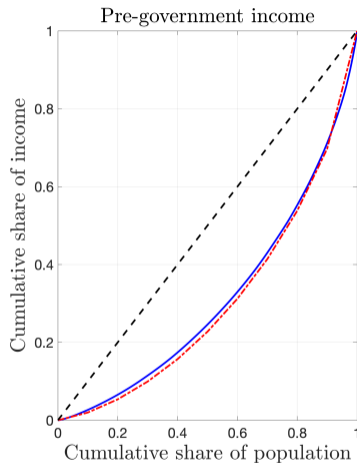
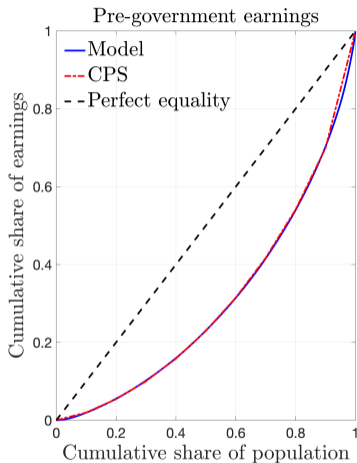
- Human capital accumulation in the model achieves a good fit of age-earnings profiles

Model fit: Residual variation in earnings



- Idios. shocks match well the increase of earnings heterogeneity over the life-cycle

Model fit: Inequality (Lorenz curves)



- Model achieves a good fit of pre-government earnings and income distributions
- We calibrate altruism (ϕ_1, ϕ_2, η) to match the distribution of bequests [▶ Bequest distribution](#)

Quantitative Experiments

Quantitative experiments

- Unanticipated, permanent, an potentially joint social security and income tax reforms:
 - New pension system is only applied to agents that are currently working
 - New pension system is phased in linearly during forty years. \Rightarrow Only a new labor market entrant takes full advantage.
 - New income tax system applies to everyone immediately
 - Average income tax rate adjusts every period to satisfy the government budget
 - Payroll taxes adjust every period to make sure the Social Security budget is satisfied
- We compute the full transition to the new steady state for all reforms

Social Welfare Function

- The initial (calibrated) policy is Λ^0
- At time t , government chooses constant future policy $\Lambda^* = (\bar{\lambda}_{SS}, \lambda_{SS}, \lambda_I)$ given by:

$$\Lambda^* = \arg \max_{\Lambda} W(\Lambda^0, \Lambda)$$

- Two Social Welfare Functions:
 - Current Cohorts:

$$CG : W = \underbrace{\sum_j \int V_t(\mathbf{x}; \Lambda^0, \Lambda) dF_{t,j}}_{\text{welfare of current generations}}$$

- Newborn in a Final Steady State

$$FG : W = \underbrace{\int V_{\infty}(\mathbf{x}^{nb}; \Lambda^0, \Lambda) dF_{\infty, j=1}}_{\text{welfare of long run newborn}}$$

Constraints

- Given the initial conditions, the new policy triggers a new **equilibrium** (transition to a new steady state).
- The government may face some "Pareto Constraints" when setting the policies:
 - No current cohort is worse off:

$$\int V_t(\mathbf{x}; \Lambda^0, \Lambda) dF_{t,j} \geq \int V_t(\mathbf{x}; \Lambda^0, \Lambda^0) dF_{t,j} \quad \forall j$$

- No future cohort is worse off:

$$\int V_t(\mathbf{x}^{nb}; \Lambda^0, \Lambda) dF_{t,j=1} \geq \int V_t(\mathbf{x}^{nb}; \Lambda^0, \Lambda^0) dF_{t,j=1} \quad \forall t > 1$$

Findings

Optimal policy

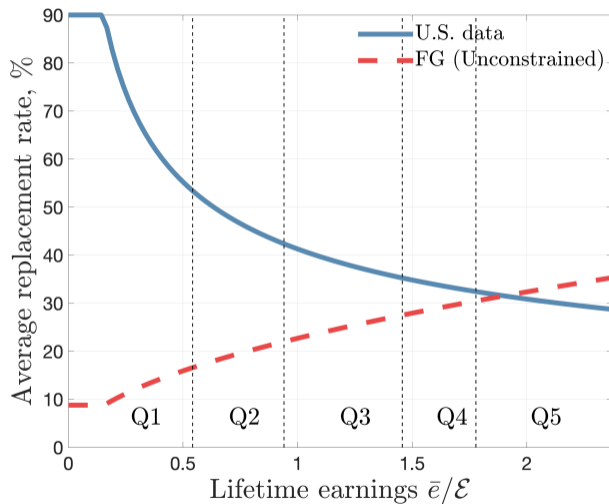
	Joint policy			CEV, %	
	$\bar{\lambda}_{SS}$	λ_{SS}	λ_I	Alive	Future
Status Quo	0.413	1.420	0.216	-	-

Optimal policy

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	$\bar{\lambda}_{SS}$	λ_{SS}	λ_I	Alive	Future
Status Quo	0.413	1.420	0.216	–	–
Objective: Long Run Welfare (FG)					
– Unconstrained	0.227	0.488	0.221	-3.519	2.314

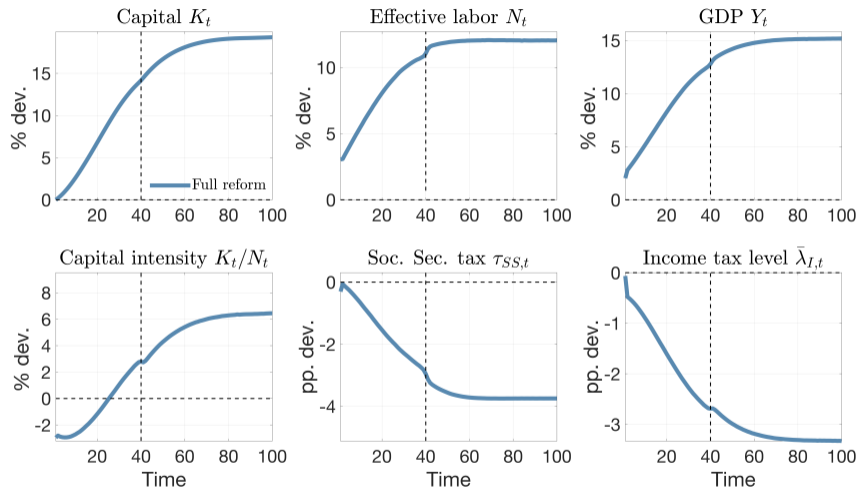
- Redistribution/Insurance has declined (slightly increased) through the pension system (tax system).
- Welfare gains are much higher than those that can be achieved by income tax reforms.

Average replacement rates



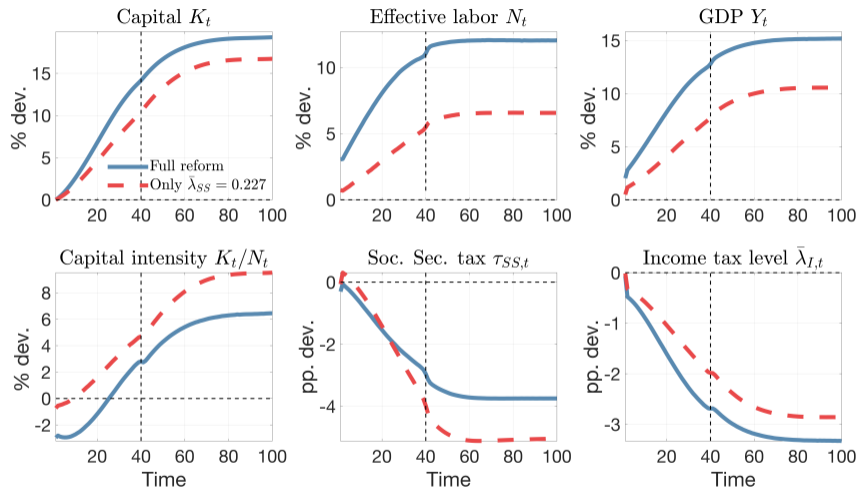
- Not generous and regressive pension system

Aggregate variables and prices



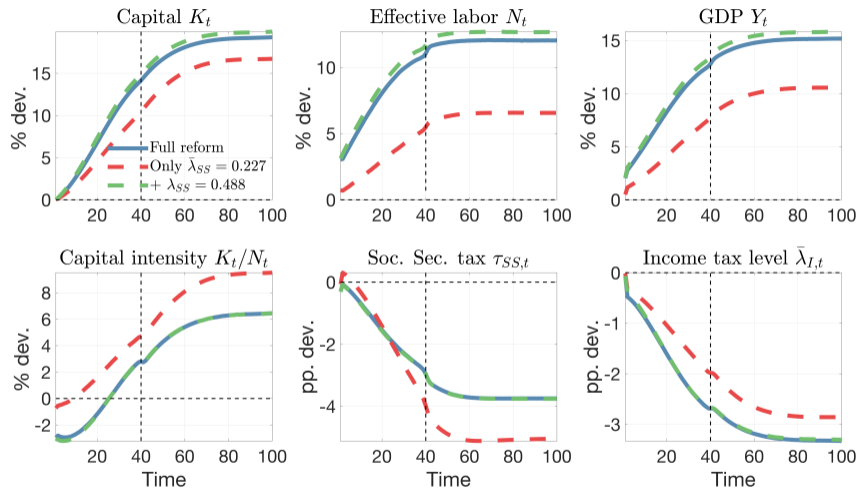
- Reform reduces distortions and hence increases output/consumption in the long run.

Aggregate variables and prices



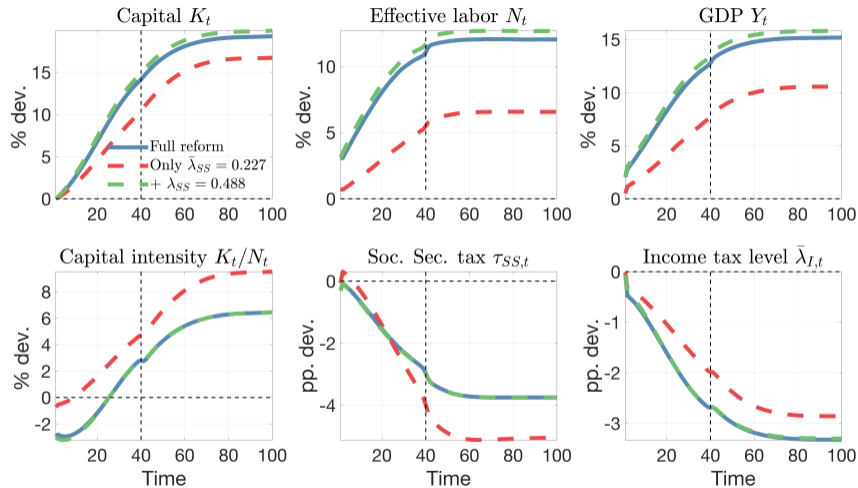
- Reduced level of pensions lowers distortions on savings and on labor supply.

Aggregate variables and prices



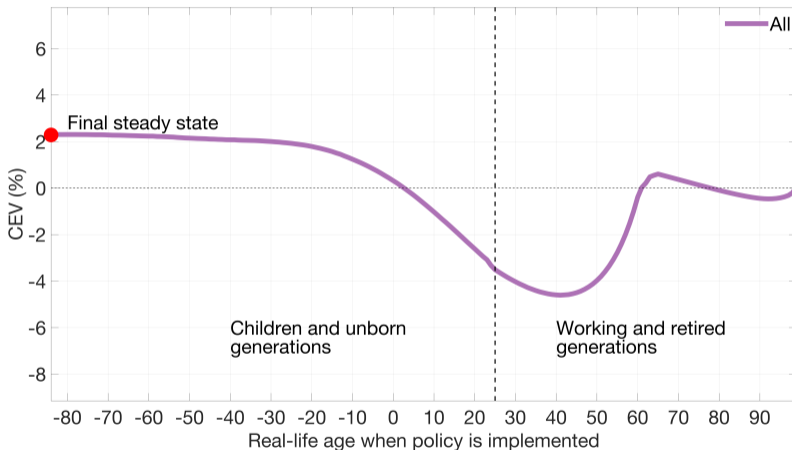
- Regressive pension system boosts labor supply further.

Aggregate variables and prices



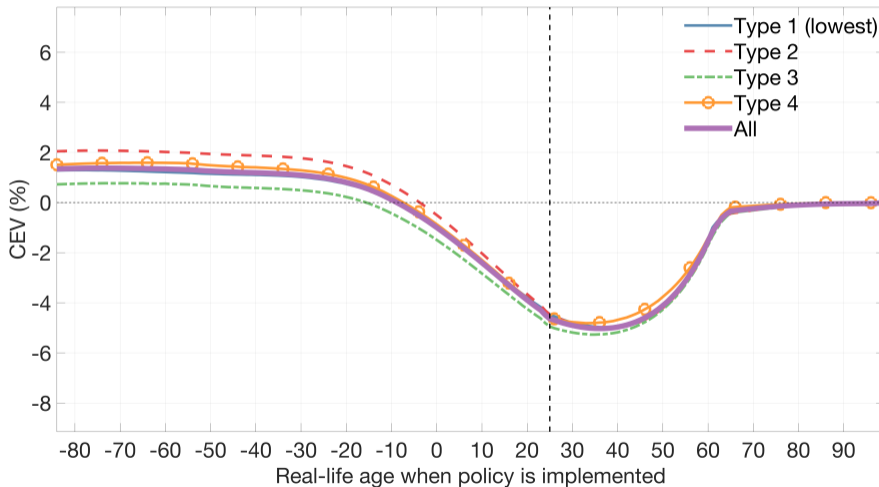
- Less redistribution through the pension system requires slightly more redistribution through the income tax system.

Welfare effects by cohort (CEV, %)

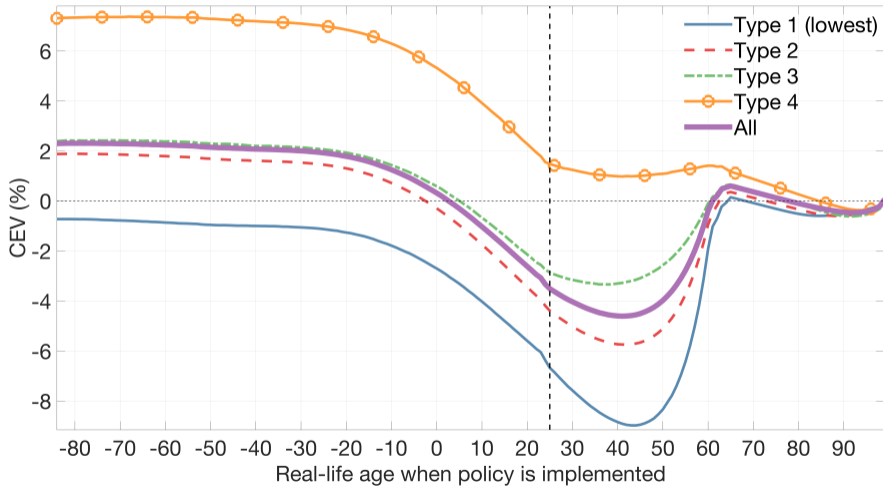


- Reform benefits future cohorts at the welfare cost of current generations

Only pension generosity $\bar{\lambda}_{SS} = 0.227$



Full reform

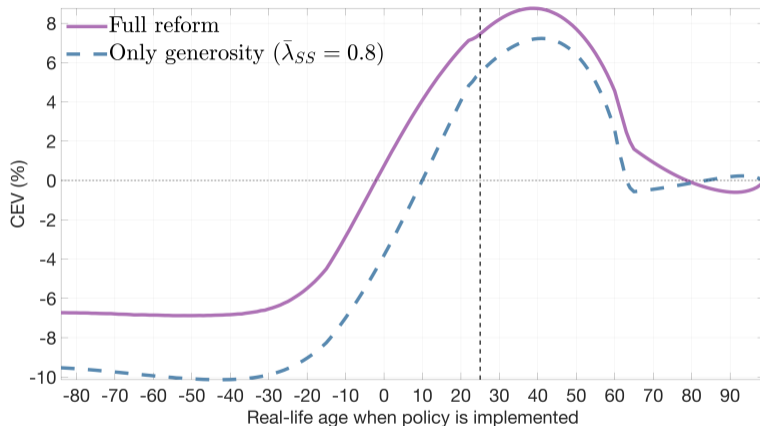


Optimal policy

	Joint policy			CEV, %	
	$\bar{\lambda}_{SS}$	λ_{SS}	λ_I	Alive	Future
Status Quo	0.413	1.420	0.216	–	–
Objective: Long Run Welfare (FG)					
– Unconstrained	0.227	0.488	0.221	-3.519	2.314
Objective: Current Generations (CG)					
– Unconstrained	0.800	0.40	0.184	7.426	-6.730

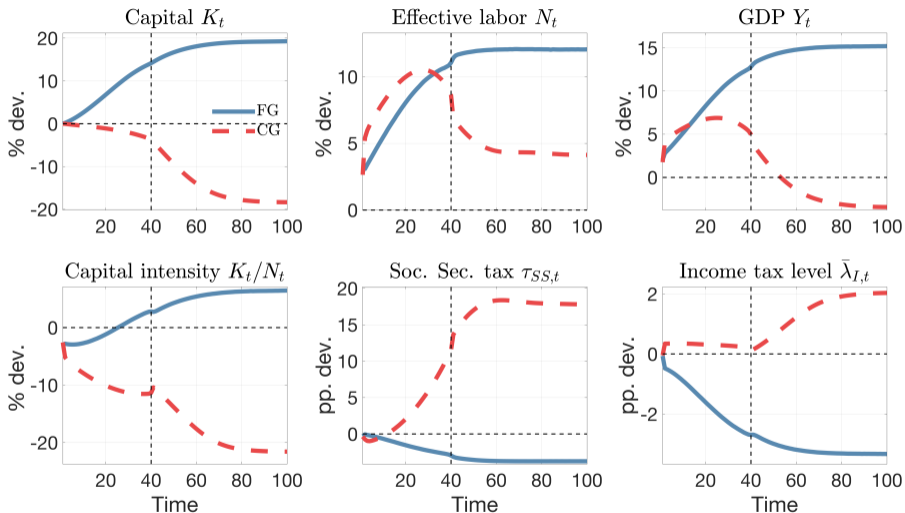
- Pension generosity Doubles.

Inter-generational redistribution



- Pension generosity $\bar{\lambda}_{SS}$ achieves most welfare gains for alive cohorts .

Aggregate variables and prices



- Current generations transfer resources from the (distant) future.

Optimal policy

	Joint policy			CEV, %	
	$\bar{\lambda}_{SS}$	λ_{SS}	λ_I	Alive	Future
Status Quo	0.413	1.420	0.216	–	–
Objective: Long Run Welfare (FG)					
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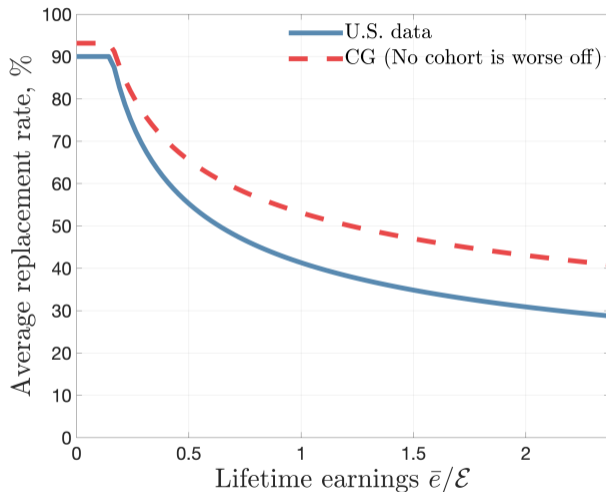
- Is it feasible to design reform that maximizes the welfare of alive and does not make **any** cohort, on average, worse off?

Optimal policy

	Joint policy			CEV, %	
	$\bar{\lambda}_{SS}$	λ_{SS}	λ_I	Alive	Future
Status Quo	0.413	1.420	0.216	–	–
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Objective: Current Generations (CG)					
– Unconstrained	0.800	0.40	0.184	7.426	-6.730
– No cohort is worse off	0.531	1.303	0.140	2.558	0.106

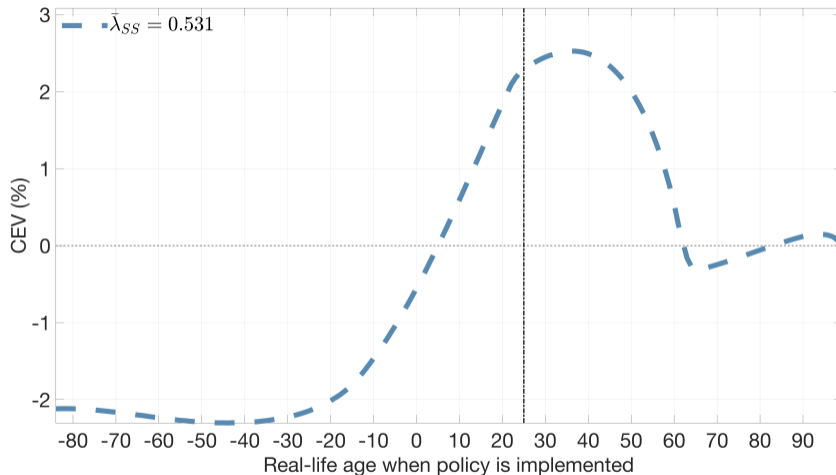
- Is it feasible to design reform that maximizes the welfare of alive and does not make **any** cohort, on average, worse off? **YES**

Average replacement rates



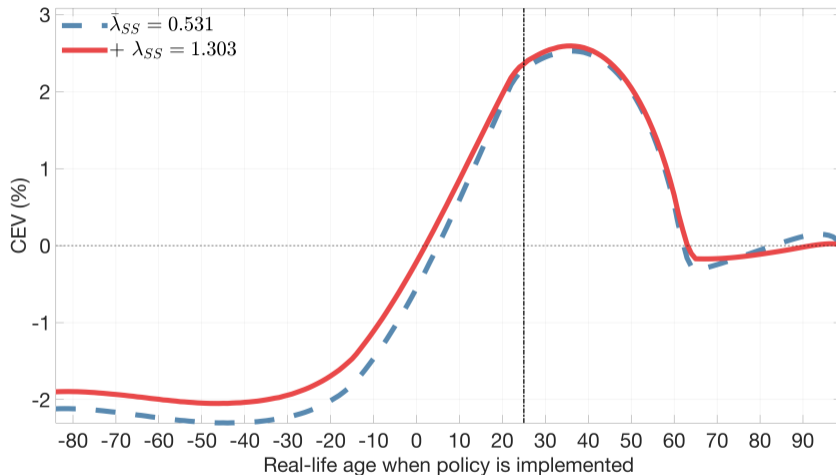
- Slightly more generous and less progressive pension system

Welfare effects: Decomposition



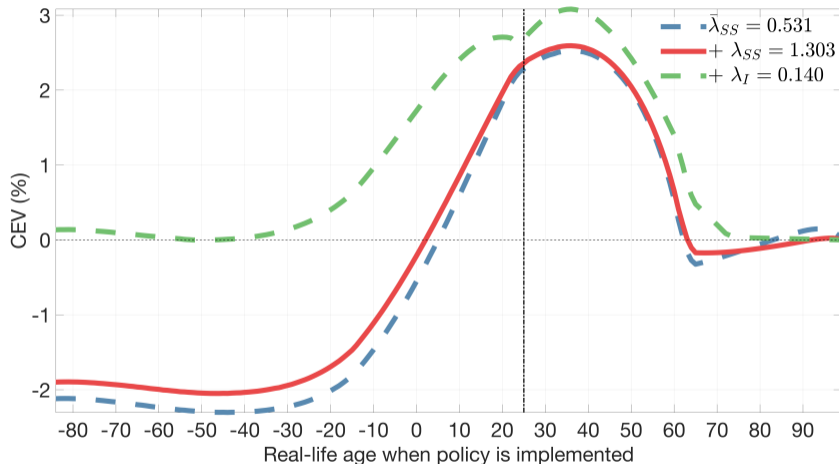
- Generosity is distortionary and cannot achieve Pareto-improvement across all cohorts

Welfare effects: Decomposition



- Less progressive pension system boosts economy in the long run

Welfare effects: Decomposition



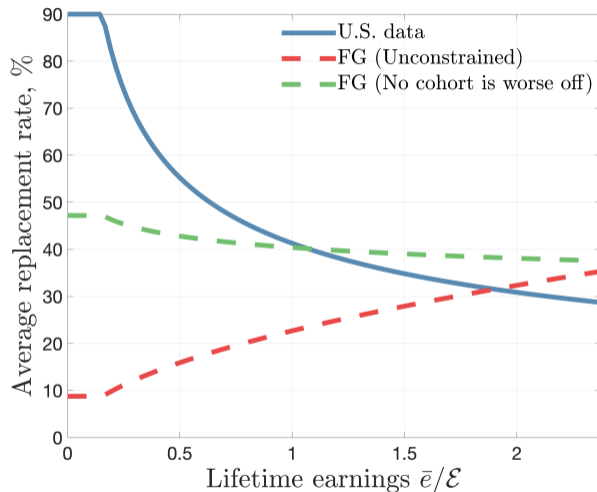
- Providing more insurance/redistribution through the pension system allows to provide less insurance/redistribution in the income tax system

Optimal policy

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Objective: Long Run Welfare (FG)					
– Unconstrained	0.227	0.488	0.221	-3.519	2.314
– No cohort is worse off	0.404	1.084	0.169	0.203	1.111
Objective: Current Generations (CG)					
– Unconstrained	0.800	0.40	0.184	7.426	-6.730
– No cohort is worse off	0.531	1.303	0.140	2.558	0.106

- There exist reforms of the pension system that make all current and future cohorts, on average, better off (regardless of the SWF)

Average replacement rates



- Reducing distortion through all channels brings all current cohorts on board.

Optimal joint policy

	Joint policy			CEV, %	
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Objective: Long Run Welfare (FG)					
– Unconstrained	0.227	0.488	0.221	-3.519	2.314
– No cohort is worse off	0.404	1.084	0.169	0.203	1.111
– No Type 1 is worse off	0.285	2.100	0.159	-2.285	1.362
– No current type is worse off	0.448	1.535	0.185	0.887	0.272
Objective: Current Generations (CG)					
– Unconstrained	0.800	0.400	0.184	7.426	-6.730
– No cohort is worse off	0.531	1.303	0.140	2.558	0.106
– No Type 1 is worse off	0.603	2.026	0.175	3.156	-3.839
– No future type is worse off	0.427	1.643	0.181	0.442	0.426

Takeaways

- Unconstrained reforms make extreme changes in generosity, causing large intergenerational redistribution; distortions reduce by lowering pension progressivity.
- When redistribution across generations is limited, the direction of pension system redesign is the same, but less redistribution through the tax system is needed.
- When redistribution “in the wrong direction” needs to be avoided, pension progressivity becomes the desirable instrument.
- When both intergenerational and cross-sectional redistribution is limited, pension progressivity increases, compensated by a significant decline in tax progressivity.
- In all cases, the joint redesign of the pension and the tax system brings much larger welfare gains than only reoptimising the tax system.

Political support

Reform	Support, %
Objective: Long Run Welfare (FG)	
– Unconstrained	34.3
– No cohort is worse off	57.5
– No Type 1 is worse off	21.4
– No future type is worse off	16.4
– No current type is worse off	82.9
Objective: Current Generations (CG)	
– Unconstrained	81.5
– No cohort is worse off	73.4
– No Type 1 is worse off	62.2
– No future type is worse off	73.3
– No current type is worse off	88.2

Optimal pension redesign

	Pension redesign			CEV, %	
	$\bar{\lambda}_{SS}$	λ_{SS}	λ_I	Alive	Future
Status Quo	0.413	1.420	0.216	–	–
Objective: Long Run Welfare (FG)					
– Unconstrained	0.210	0.499	0.216	-4.049	2.250
– No cohort is worse off	0.405	0.492	0.216	0.455	0.523
– No Type 1 is worse off	0.263	2.300	0.216	-3.519	-0.740
– No future type is worse off	0.232	1.029	0.216	-3.895	1.869
– No current type is worse off	0.485	1.408	0.216	1.309	-1.159
Objective: Current Generations (CG)					
– Unconstrained	0.800	0.400	0.216	7.293	-7.551
– No cohort is worse off	0.435	0.423	0.216	1.101	0.059
– No Type 1 is worse off	0.571	1.863	0.216	2.189	-4.960
– No future type is worse off	0.416	1.419	0.216	0.052	0.062
– No current type is worse off	0.800	0.400	0.216	7.293	-7.551

Conclusions

- The optimal joint pension and tax policy critically depends on the social welfare criterion.
- When both intergenerational and within generation redistribution is limited, the optimal policy increases pension progressivity and reduces income tax progressivity.
- The welfare gains from only adjusting the tax or the pension system are significantly smaller compared to the joint design.

Next Steps

- Examine how particular elements of the tax/pension system (cap, tax credit for SS contributions, taxation of pensions, early retirement) affect our optimal policies.
- Analyse more where the distortions are coming from: labor supply/human capital vs. life-cycle savings and how they interact with redistribution needs.
- Is there a chance for a fully Pareto optimal reform?
- Why pension progressivity is more distortionary than income tax progressivity?

Optimal Income Redistribution

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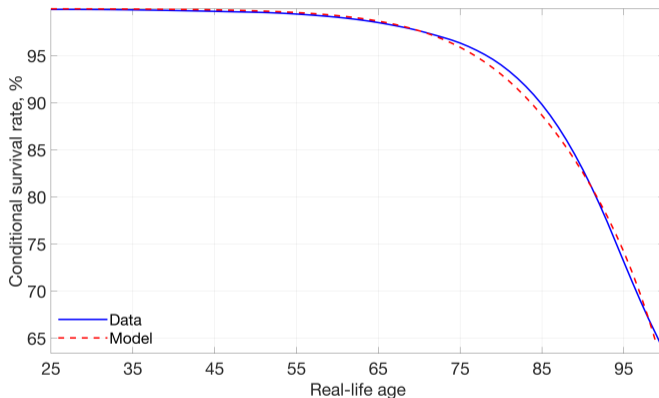
Pavel Brendler
University of Bonn

Eva Cárceles-Poveda
Stony Brook University

HANK Prague, May 17, 2024

Appendix

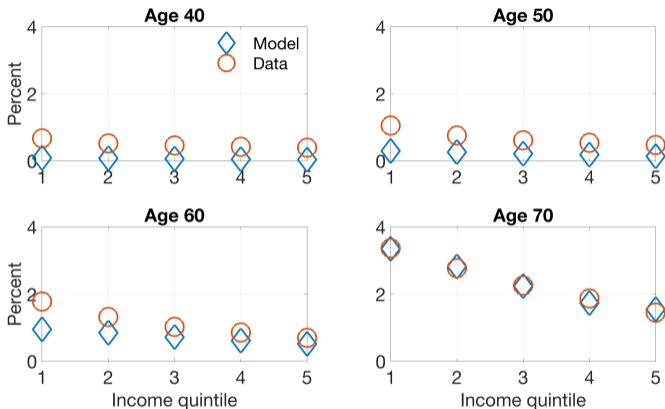
Survival probability rates



Conditional survival probability rates in the model and data

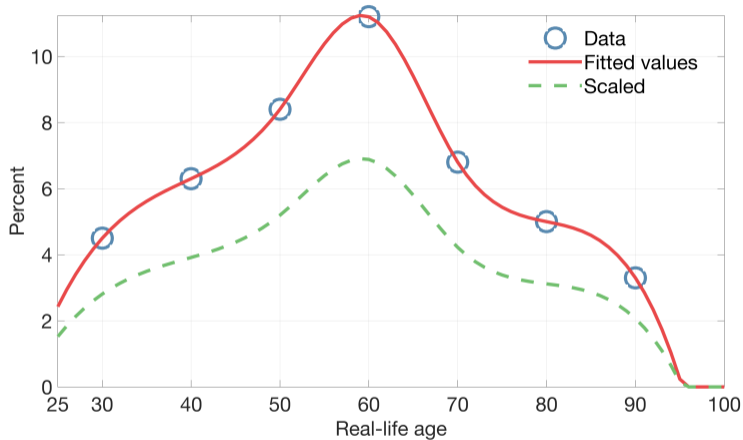
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Mortality rates



Conditional mortality rates by income in the model and data [▶ Back](#)

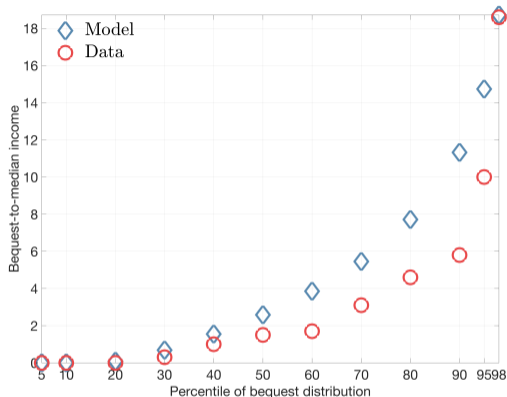
Bequest distribution



Age profile of probabilities to receive a bequest in the model and data [▶ Back](#)

Notes: Empirical data comes from SCF (2001–2019).

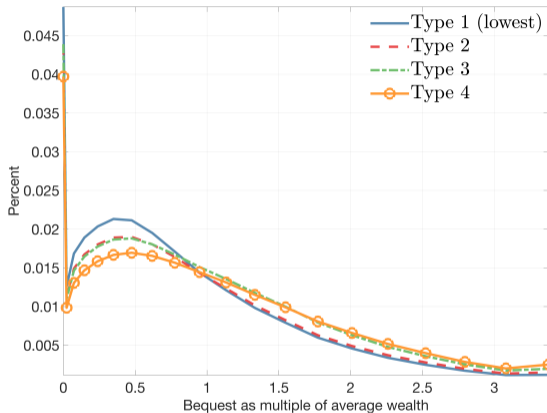
Bequest distribution



Bequest distribution in the model and data [▶ Back](#)

Notes: Bequests are normalized by the economy-wide median pre-government income. Empirical data comes from Hurd and Smith (2001).

Bequest distribution



Bequest distribution by type in the model [▶ Back](#)

Notes: Bequests are normalized by the economy-wide average wealth.